



Name : .....  
Roll No. : .....  
Invigilator's Signature : .....

**CS/BCA/SEM-3/BM-301/2011-12**

**2011**

**MATHEMATICS FOR COMPUTING**

Time Allotted : 3 Hours

Full Marks : 70

*The figures in the margin indicate full marks.*

*Candidates are required to give their answers in their own words  
as far as practicable.*

**GROUP – A**

**( Multiple Choice Type Questions )**

1. Choose the correct alternatives for any *ten* of the following :

10 × 1 = 10

- i) The mathematical model of a Mealy Machine is a
  - a) 5-tuple
  - b) 4-tuple
  - c) 6-tuple
  - d) none of these.
- ii) A regular language is accepted by
  - a) every DFA
  - b) every NFA
  - c) no DFA
  - d) at least one DFA.
- iii) How many bit strings of length 10 contain exactly four 1's ?
  - a) 120
  - b) 720
  - c) 210
  - d) 386.





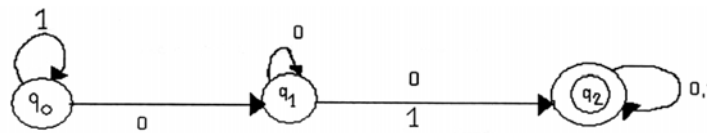
x) The type-3 grammar in relation to the automata theory is known as

- a) context sensitive grammar
- b) regular grammar
- c) context free grammar
- d) none of these.

xi) If  $n! = x(n-2)!$  then  $x =$

- a)  $n$
- b)  $n - 1$
- c)  $n(n-2)$
- d)  $n(n-1)$ .

xii) The automata



accepts the string

- a) 111
- b) 01
- c) 11
- d) none of these.

xiii) The generation function for the sequence 1, 2, 3, 4 ... is

- a)  $(1+2x)^{-1}$
- b)  $(1-2x)^{-1}$
- c)  $(1-x)^{-2}$
- d)  $(1+x)^{-2}$ .





7. Construct the graph or digraph corresponding to the following incidence matrix :

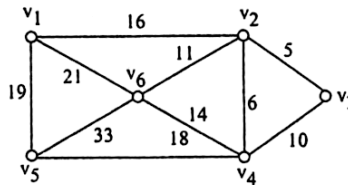
$$\begin{pmatrix} 1 & 0 & 0 & 0 & 0 & 1 \\ 0 & 1 & 1 & 0 & 1 & 0 \\ 1 & 0 & 0 & 1 & 0 & 0 \\ 0 & 1 & 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 1 & 1 \end{pmatrix}$$

**GROUP - C**

**( Long Answer Type Questions )**

Answer any *three* of the following.  $3 \times 15 = 45$

8. a) Write Kruskal's Algorithm for minimal spanning tree.  
 b) Find the minimal spanning tree of the following labelled connected graph by Kruskal's Algorithm.



- c) How many permutations can be made out of the letters of the word 'Basic' that  
 i) begin with B ?  
 ii) end with C ?  $5 + 5 + 5$
9. a) Write CNF & DNF of the following statement :  
 $p \rightarrow ( p \wedge ( q \rightarrow p ) )$
- b) Verify whether the argument given below is valid or not :  
 If I like Mathematics then I will study.  
 Either I do not study or I pass the examination.  
 If I do not graduate then I did not pass Mathematics.  
 ... If I like Mathematics, then I will graduate.



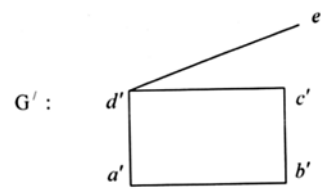
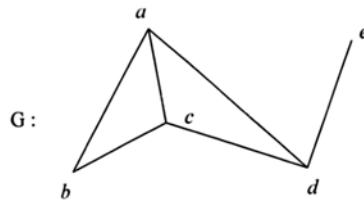
c) Prove the following equivalence :

$$p \Leftrightarrow (p \wedge q) \vee (p \wedge \sim q)$$

10. a) Draw the graph represented by the given adjacency matrix :

$$\begin{pmatrix} 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \end{pmatrix}$$

b) Examine if the following two graphs are isomorphic :



8 + 7

11. a) Prove that the number of vertices of odd degree in a graph is always even.

b) Show that  $(2n)! = 2^n \cdot n! \{ 1, 3, 5, \dots, (2n-1) \}$ .

c) In how many ways can three prizes be distributed among 4 boys when,

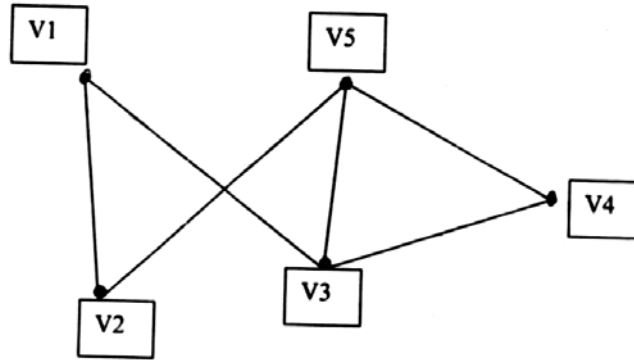
i) no one gets more than one prize ?

ii) a boy can get any number of prizes ? 5 + 5 + 5



12. a) Solve  $a_n - 5a_{n-1} + 6a_{n-2} = 0$ , where  $a_0 = 2, a_1 = 5$ .

b) Find the incidence matrix of the following graph :



7 + 8

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