



v) $A \cap B^c =$

a) $A - B$

b) $(A \cup B)^c$

c) $A - B^c$

d) none of these.

vi) If $A = \{1, 2, 3\}$, $B = \{4, 5\}$, $C = \{1, 2, 3, 4, 5\}$, then $(C \times B) - (A \times B) =$

a) $(C - A) \times (B - A)$

b) $B \times B$

c) $(C \cap A) \times B$

d) none of these. vii) If A and B are two fuzzy sets given by

$$A = \{(1, 0.1), (3, 0.4), (5, 0.2), (7, 0.8)\} \text{ and}$$

$$B = \{(1, 0.3), (3, 0.2), (5, 0.5), (7, 0.7)\} \text{ then}$$

a) $A \cup B = \{(1, 0.3), (3, 0.4), (5, 0.2), (7, 0.8)\}$

b) $A = \{(1, 0.1), (3, 0.4), (5, 0.5), (7, 0.8)\}$

c) $A \cup B = \{(1, 0.3), (3, 0.4), (5, 0.5), (7, 0.8)\}$

d) none of these. viii) If the function $f: R \rightarrow R$ defined by

$$f(x) = \begin{cases} 3x - 4, & x > 0 \\ -3x + 2, & x \leq 0 \end{cases}$$

then $f^{-1}(2) =$

a) $\{2\}$

b) $\{0, 2\}$

c) $\{2, -2\}$

d) none of these. ix) The generating function of the sequence $\{0, 1, 0, -1, 0, 1, 0, -1, 0, \dots\}$ is

a) $\frac{1}{1+x^2}$

b) $\frac{x}{1+x^2}$

c) $\frac{x^2}{1+x^2}$

d) none of these.



x) A complete graph of n vertices has exactly

a) $\frac{n(n+1)}{2}$ vertices

b) $\frac{n(n-1)}{2}$ vertices

c) $\frac{(n+1)}{2}$ vertices

d) none of these.

xi) Cardinality of the power set of a non-empty set A is

a) $2^{|A|}$

b) $2|A|$

c) $|A|^2$

d) none of these.

xii) The solution of the recurrence relation

$$a_r - 7a_{r-1} + 10a_{r-2} = 0 \text{ given } a_0 = 0, a_1 = 3 \text{ is}$$

a) $a_r = 5^r - 2^r$

b) $5^r + 2^r$

c) $5^r - 2^r$

d) none of these.

GROUP - B

(Short Answer Type Questions)

Answer any three of the following.

$3 \times 5 = 15$

2. Solve the following using generating function :

$$a_n - a_{n-1} = 3(n-1), \quad n \geq 1, \text{ and where } a_0 = 2.$$

3. Find the coefficient of x^{18} in $(x + x^2 + x^3 + x^4 + x^5)(x^2 + x^3 + x^4 + x^5 + \dots)^5$.

4. Let A be some fixed 10-element subset of $S = \{1, 2, 3, 4, 5, \dots, 50\}$. Show that A possesses two different 5-element subsets, the sums of whose elements are equal.

5. Show that $4^{2n+1} + 3^{n+2}$ is an integer multiple of 13, for all positive integers n .

6. Draw the graph represented by the given adjacency matrix :

$$\begin{pmatrix} 1 & 2 & 0 & 1 \\ 2 & 0 & 3 & 0 \\ 0 & 3 & 1 & 1 \\ 1 & 0 & 1 & 0 \end{pmatrix}$$



v) $A \cap B^c =$

a) $A - B$

b) $(A \cup B)^c$

c) $A - B^c$

d) none of these.

vi) If $A = \{1, 2, 3\}$, $B = \{4, 5\}$, $C = \{1, 2, 3, 4, 5\}$, then $(C \times B) - (A \times B) =$

a) $(C - A) \times (B - A)$

b) $B \times B$

c) $(C \cap A) \times B$

d) none of these.

vii) If A and B are two fuzzy sets given by

$$A = \{(1, 0.1), (3, 0.4), (5, 0.2), (7, 0.8)\}$$
 and

$$B = \{(1, 0.3), (3, 0.2), (5, 0.5), (7, 0.7)\}$$
 then

a) $A \cup B = \{(1, 0.3), (3, 0.4), (5, 0.2), (7, 0.8)\}$

b) $A = \{(1, 0.1), (3, 0.4), (5, 0.5), (7, 0.8)\}$

c) $A \cup B = \{(1, 0.3), (3, 0.4), (5, 0.5), (7, 0.8)\}$

d) none of these.

viii) If the function $f: R \rightarrow R$ defined by

$$f(x) = \begin{cases} 3x - 4, & x > 0 \\ -3x + 2, & x \leq 0 \end{cases}$$

then $f^{-1}(2) =$

a) $\{2\}$

b) $\{0, 2\}$

c) $\{2, -2\}$

d) none of these.

ix) The generating function of the sequence $\{0, 1, 0, -1, 0, 1, 0, -1, 0, \dots\}$ is

a) $\frac{1}{1+x^2}$

b) $\frac{x}{1+x^2}$

c) $\frac{x^2}{1+x^2}$

d) none of these.



x) A complete graph of n vertices has exactly

- a) $\frac{n(n+1)}{2}$ vertices b) $\frac{n(n-1)}{2}$ vertices
 c) $\frac{(n+1)}{2}$ vertices d) none of these.

xi) Cardinality of the power set of a non-empty set A is

- a) $2^{|A|}$ b) $2|A|$
 c) $|A|^2$ d) none of these.

xii) The solution of the recurrence relation

$$a_r - 7a_{r-1} + 10a_{r-2} = 0 \text{ given } a_0 = 0, a_1 = 3 \text{ is}$$

- a) $a_r = 5^{-r} - 2^r$ b) $5^r + 2^r$
 c) $5^r - 2^r$ d) none of these.

GROUP - B

(Short Answer Type Questions)

Answer any three of the following.

3 × 5 = 15

2. Solve the following using generating function :

$$a_n - a_{n-1} = 3(n-1), \quad n \geq 1, \text{ and where } a_0 = 2.$$

3. Find the coefficient of x^{18} in $(x + x^2 + x^3 + x^4 + x^5)(x^2 + x^3 + x^4 + x^5 + \dots)^5$.

4. Let A be some fixed 10-element subset of $S = \{1, 2, 3, 4, 5, \dots, 50\}$. Show that A possesses two different 5-element subsets, the sums of whose elements are equal.

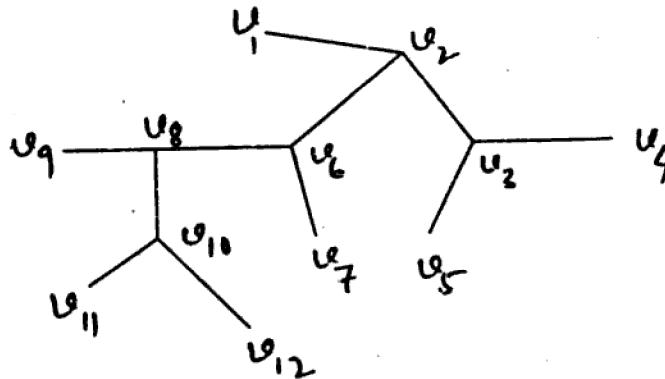
5. Show that $4^{2n+1} + 3^{n+2}$ is an integer multiple of 13, for all positive integers n .

6. Draw the graph represented by the given adjacency matrix :

$$\begin{pmatrix} 1 & 2 & 0 & 1 \\ 2 & 0 & 3 & 0 \\ 0 & 3 & 1 & 1 \\ 1 & 0 & 1 & 0 \end{pmatrix}$$



7. Find the generating function for the sequence 1 1 0 1 1 1 1
8. Explain the Ring Sum operation with an example. Find the centre of the following graph :



GROUP - C

(Long Answer Type Questions)

Answer any three of the following questions.

3 × 15 = 45

9. Let R and S be two fuzzy relations from X to Y given in the following matrix forms. Find (a) $R \cup S$, (b) $R \cap S$, (c) $R + S$ and (d) $R \cdot S$.

$$M_R = \begin{matrix} & y_1 & y_2 & y_3 \\ \begin{matrix} x_1 \\ x_2 \end{matrix} & \begin{pmatrix} 0.3 & 1 & 0.2 \\ 0.8 & 0 & 0.5 \end{pmatrix} \end{matrix}$$

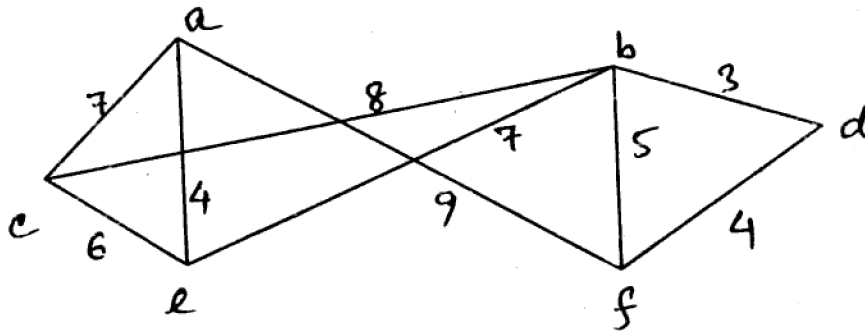
$$M_S = \begin{matrix} & y_1 & y_2 & y_3 \\ \begin{matrix} x_1 \\ x_2 \end{matrix} & \begin{pmatrix} 0.6 & 0.1 & 0.9 \\ 0 & 0.2 & 0.3 \end{pmatrix} \end{matrix}$$

Draw Hasse-diagram to illustrate the following partial ordering :

The set of all subsets of { 1, 2, 3, 4 } having at least two numbers partially ordered by \subseteq . Show that $\lfloor 2x \rfloor = \lfloor x \rfloor + \lfloor x + 1/2 \rfloor$ where x is a real number. 8 + 5 + 2



10. Prove that a simple graph with n vertices and k components can have at most $(n - k)(n - k + 1) / 2$ edges. Prove that in a tree there exists one and only one path between every pair of vertices. 6 + 9
11. Find the shortest path of the following graph using Prim's algorithm :



Given the post-order and inorder traversals of a binary tree. Draw the unique binary tree :

Post-order : d e c f b h i g a

Inorder : d c e b f a h g i

8 + 7

12. a) Define grammar of a language and its types. Give an example of a grammar which is Type 2 but not Type 3. 2 + 3
- b) Find the grammar for the language $L = L = \{ w \in \{ a, b, c \}^* : w = a^n b^n c^m, n \geq 1, m \geq 0 \}$. 5
- c) Define Mealy machine and Moore Machine. Construct a Moore machine from the following Mealy machine : 5

Present State	Next State			
	a = 0		a = 1	
	State	Output	State	Output
s_0	s_0	1	s_1	0
s_1	s_3	1	s_3	1
s_2	s_1	1	s_2	1
s_3	s_2	0	s_0	1



13. a) Define a lattice. Prove that a collection of sets closed union and intersection is a lattice. 1 + 4
- b) Prove that in a bounded distributive lattice (L, \cap, \cup) an element cannot have more than one complement. 4
- c) Find the sum of all four digits of even numbers that can be made with the digits 0, 1, 2, 3, 5, 6 and 8. 6

END